## Appendix A <br> Notation

## Scalars, Vectors, and Matrices

Scalars Scalars are denoted by plain (not boldface) characters, such as $x, a, i, \mu$.
Vectors Vectors are denoted by boldface characters, so, for example, $\mathbf{x}=\left(x_{1}, x_{2}, \ldots, x_{n}\right)$.
Matrices Matrices are denoted by boldface uppercase characters, such as $\mathbf{A}=\left[a_{i j}\right]$
where $a_{i j}$ denotes the element in the $i^{\text {th }}$ row and $j^{\text {th }}$ column of $\mathbf{A}$. The $i^{\text {th }}$ row of a matrix $\mathbf{A}$ is denoted $\mathbf{A}^{i}$, and the $j^{\text {th }}$ column is denoted $\mathbf{A}_{\boldsymbol{j}}$.
Inner products The inner product of two vectors $\mathbf{x}$ and $\mathbf{y}$ is denoted $\mathbf{x}^{\top} \mathbf{y}$ and is defined by

$$
\mathbf{x}^{\top} \mathbf{y}=\sum_{i=1}^{n} x_{i} y_{i}
$$

The inner product of a matrix $\mathbf{A}$ and a vector $\mathbf{x}$ is denoted $\mathbf{A}^{\top} \mathbf{x}$ and is defined as the vector

$$
\mathbf{A}^{\top} \mathbf{x}=\left(\mathbf{A}^{1^{\top}} \mathbf{x}, \mathbf{A}^{2^{\top}} \mathbf{x}, \ldots, \mathbf{A}^{n \top} \mathbf{x}\right) .
$$

The following is a list of variables along with a description of their typical meanings throughout the text.

## Roman Variables

A Incidence matrix for a network model $\mathbf{A}=\left[a_{i j}\right]$, where $a_{i j}=1$ if resource $i$ is used by product $j$ and $a_{i j}=0$ otherwise; $m$ rows, $n$ columns.
$\mathbf{A}^{i}$ The $i^{\text {th }}$ row of the incidence matrix $\mathbf{A}$.
$A^{i}$ The set of products that use resource $i$.
$\mathbf{A}_{j}$ The $j^{\text {th }}$ column of the incidence matrix $\mathbf{A}$. Also used to denote the set of resources used by product $j$.
$A_{j}$ The set of resources used by product $j$.
$B_{j}(y, D)$ The $j^{\text {th }}$ "fill event."
$b_{j}$ Booking limit or nested booking limit.

